

# How much is in the tank? Reservoir volume uncertainty

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## Motivation

- Reserves are a major component of an energy company's value
- Estimating reserves accurately is essential

## Objective

- Make a prediction of the oil volume as well as its likelihood

# Standard techniques used in resource/reserve estimation

- SPE/WPC/AAPG/SPEE – Petroleum Resources Management System (PRMS) – 2007

“Incorporation of seismic analysis typically improves the underlying reservoir models and yields more reliable resources estimates.”

- SEC approved new reporting rules (effective January 1<sup>st</sup>, 2010)

# The Volumetric Method

Hydrocarbon in place

## Oil reservoirs

$$OOIP = \frac{7,758 \times A \times h \times \phi \times (1 - S_{wi})}{B_{oi}}$$

OOIP = Original oil in place

A = Area (acres)

h = net pay thickness (ft)

$\phi$  = porosity (fraction)

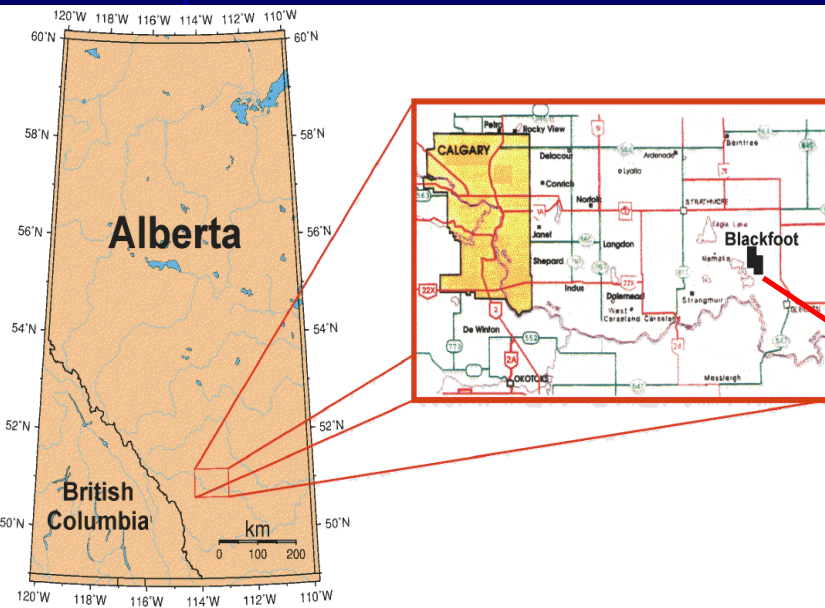
$S_{wi}$  = initial water saturation (fraction)

$B_{oi}$  = initial oil formation volume factor (rb/stb)



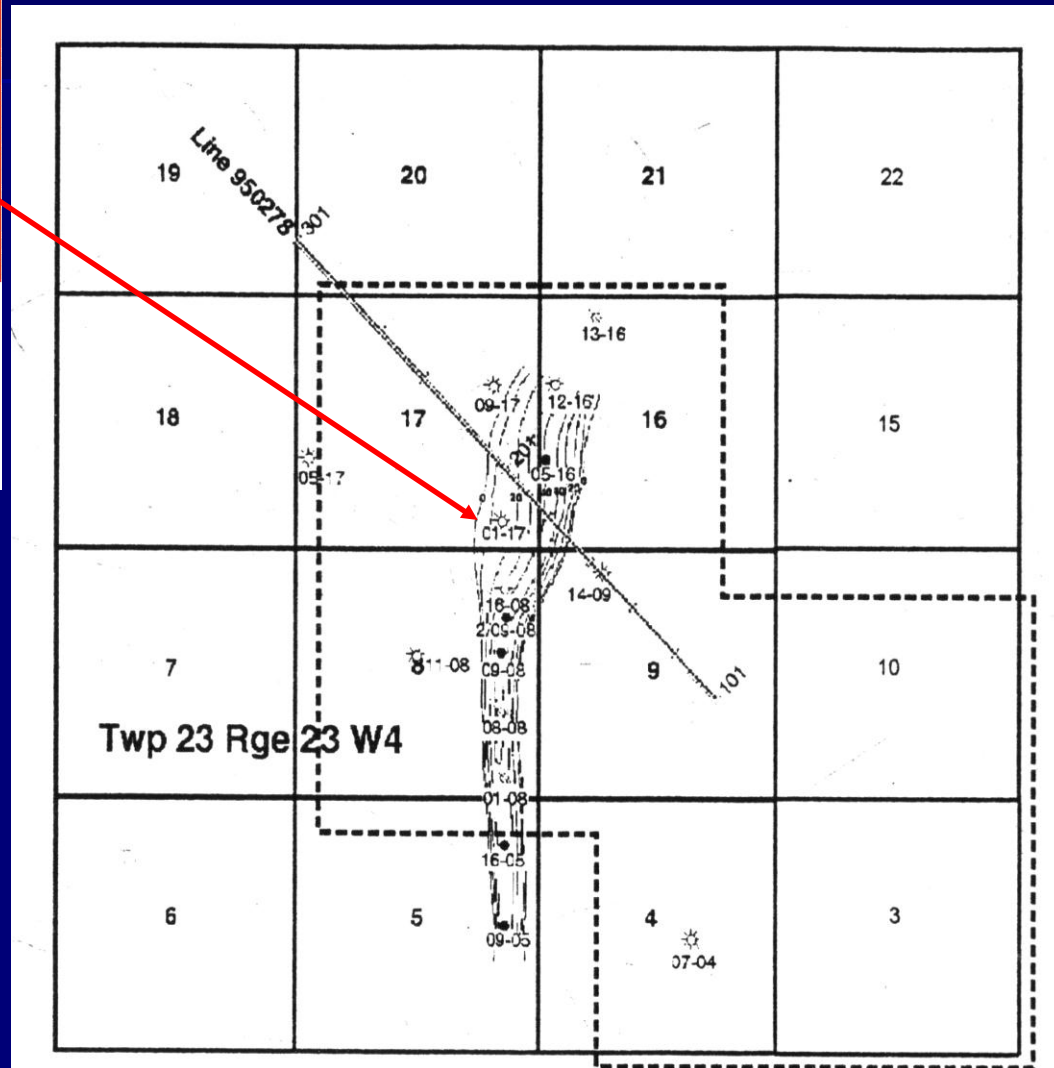
Our focus

# Blackfoot 3C-3D: location map



**HC reservoirs** are found in structural and stratigraphic traps where porous **channel sands** pinch out against non-reservoir regional strata or low-porosity sediments.

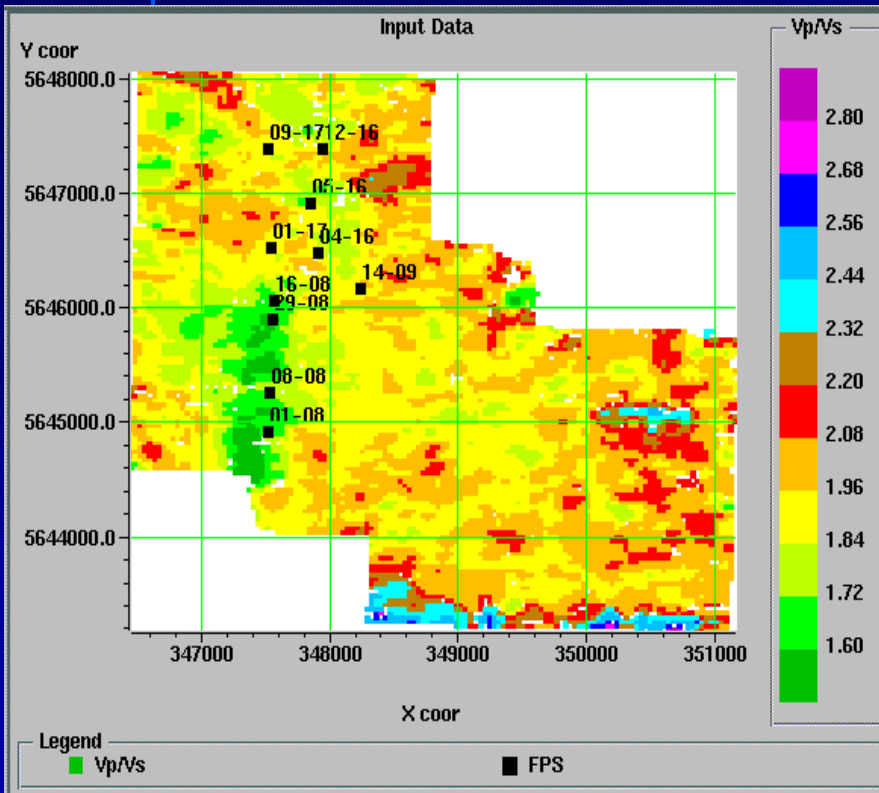
Primary HC at the field is oil, although some gas may be encountered.



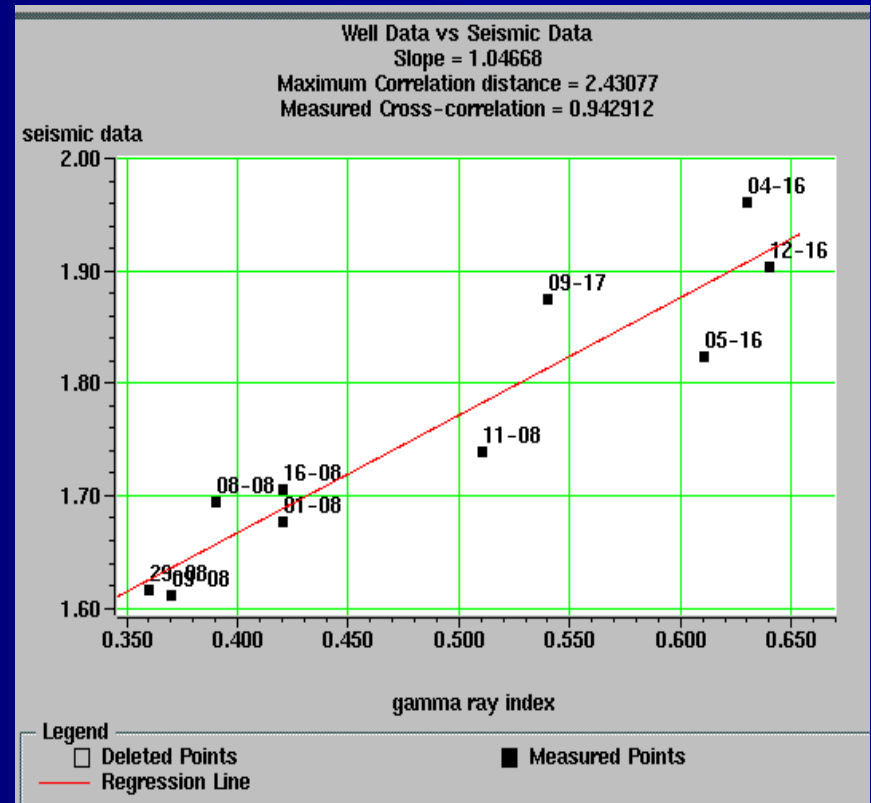
# Spreading the GRI information

## Vp/Vs distribution

From 3C-3D seismic data



## Vp/Vs vs GRI

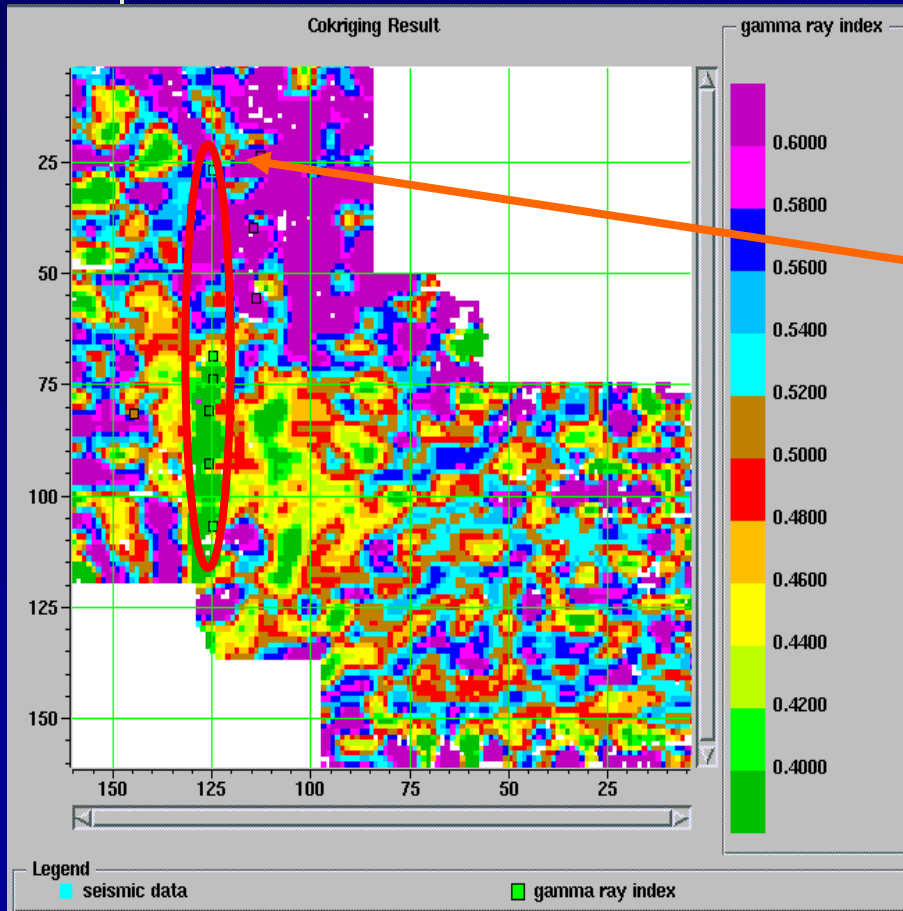


**correlation: 0.94**

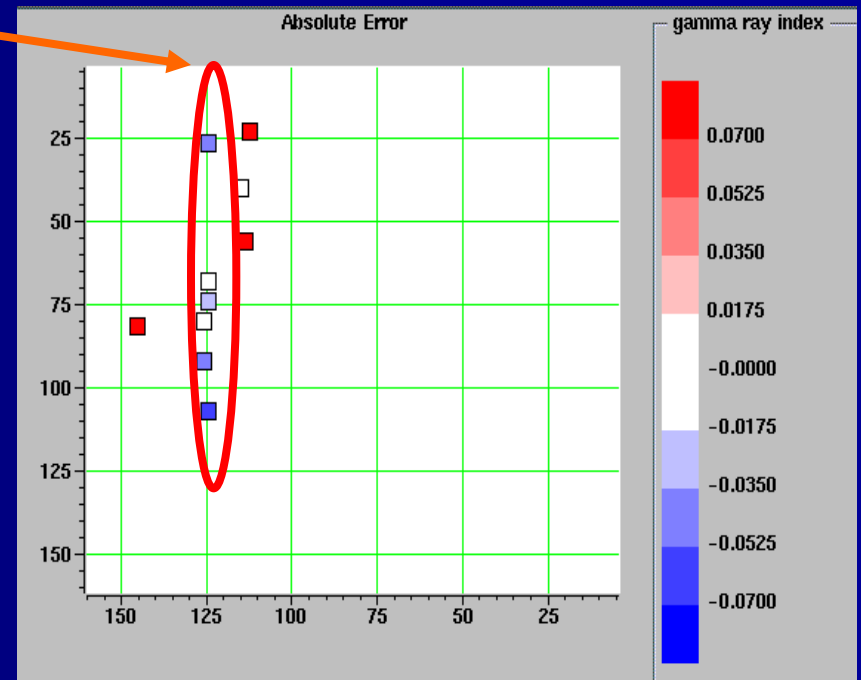
# Uncertainty in GRI cokriging



## GRI after cokriging



## Cross-validation Absolute error



# Area of the reservoir

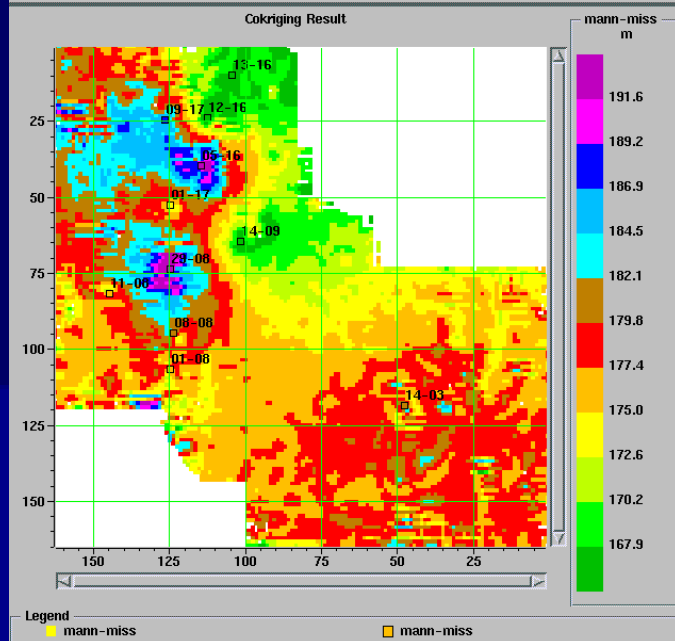


$$OV = \text{Area} * OC$$

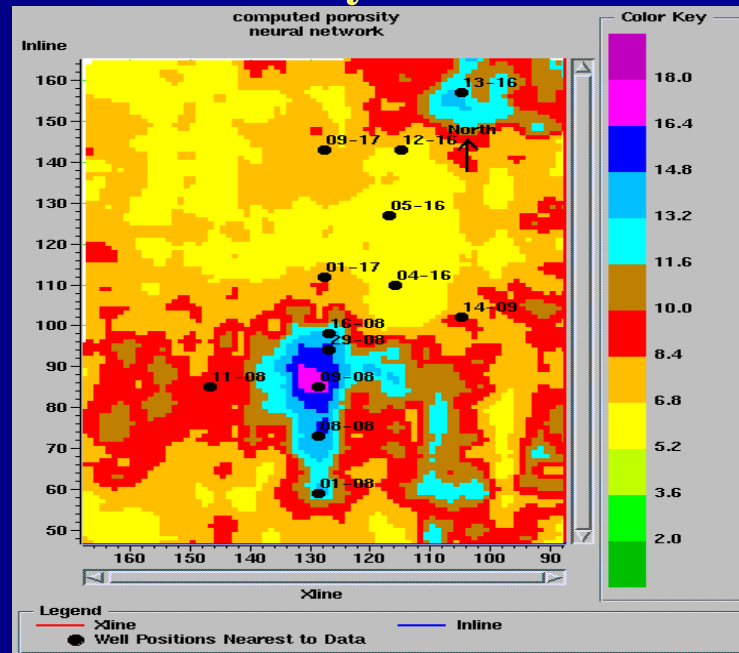
Thickness  
distribution

Area should be defined by  
(Ringrose 2007):

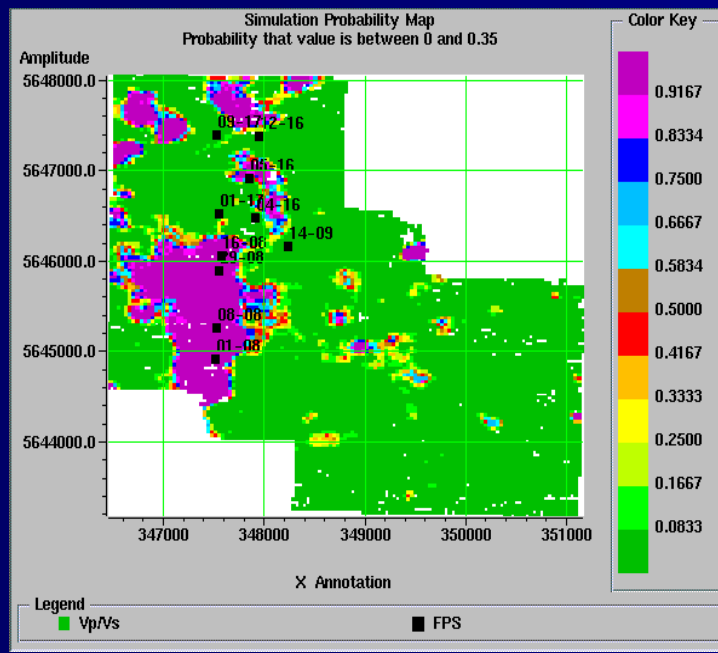
- V-shale cut off (net sand)
- Porosity cut-off (net reservoir)
- Saturation cut-off (net pay)



## Porosity distribution



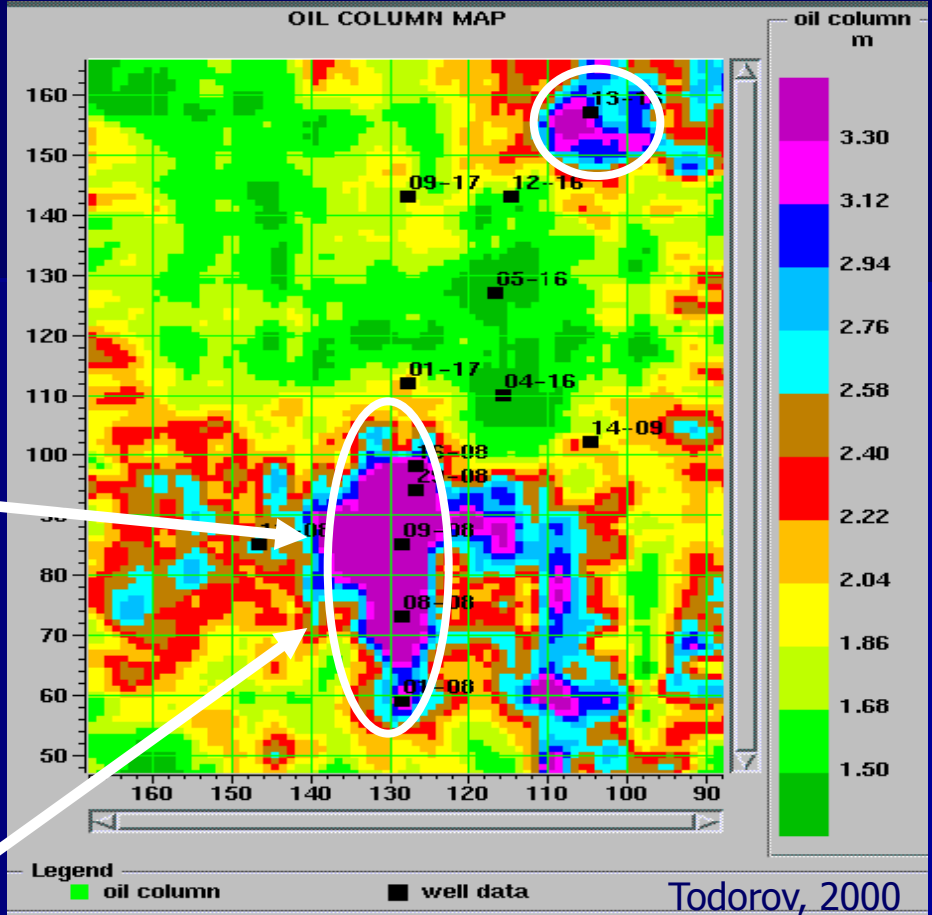
Sand  
distribution



*PCP Engineering*  
**Drain. area = 64 Ht**  
**Net Pay = 17.5m**  
**OOIP ~  $1.36 \times 10^6 \text{m}^3$**

**Seismic & Logs**  
**Area ~ 60 Ht**  
**Oil column ~ 3m**  
**Volume ~  $1.2 \times 10^6 \text{m}^3$**

Stewart 2010 **⊕ Sw = 0.25**



Oil volume predicted by Todorov

**$OV_{\text{Todorov}} \approx 7,910,000 \text{ bbl}$**



# 1<sup>st</sup> Method of estimation of uncertainty in OV

Uncertainty/Error  
quantification



Comparison of a  
measured/simulated value with  
*a reference value*

Blind wells procedure  
(cross-validation)

+

Well log data  
(reference value)

independent measurements

% Error thickness = 6%

% Error %sand = 10%


% Error porosity = 11%



Adopting that the measurements and errors are independent to each other, using  $\sigma$  as a measurement of the uncertainty

Uncertainty in OV

(Coleman & Steele, 1989)


$$\left(\frac{\sigma_{OV}}{OV}\right)^2 = \left(\frac{\sigma_{thickness}}{thickness}\right)^2 + \left(\frac{\sigma_{\%sand}}{\%sand}\right)^2 + \left(\frac{\sigma_{\phi}}{\phi}\right)^2 + \left(\frac{\sigma_{S_{HC}}}{S_{HC}}\right)^2 + \left(\frac{\sigma_{Area}}{Area}\right)^2$$

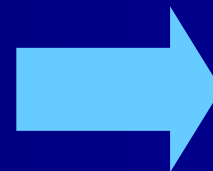
% Error thickness = 6%

% Error %sand = 10%

% Error porosity = 11%

% Error  $S_{oil}$  (from logs) = 10%

% Error Area = 15%

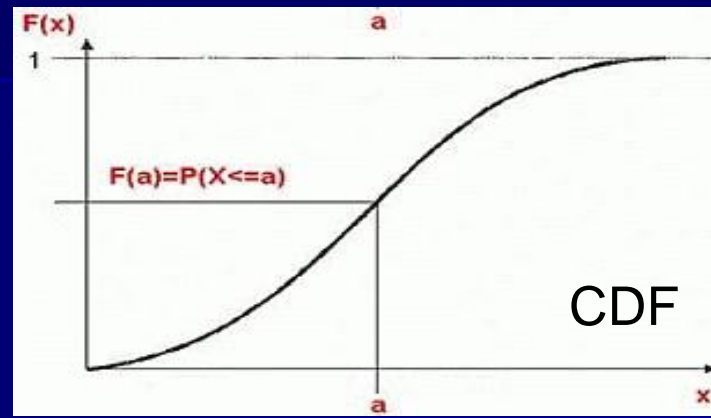
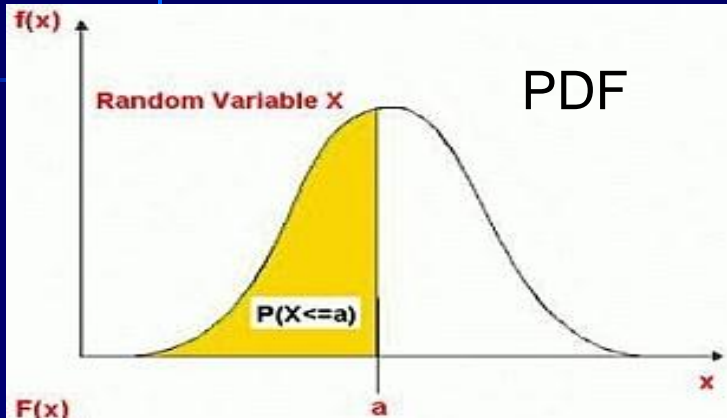


$$\frac{\sigma_{ov}}{OV} \cong 0.23$$



**Uncertainty in  
the Oil Volume**

# Exploring the PDF-CDF relationship



$$\frac{\sigma_{ov}}{ov} \cong 0.23$$

$$P_{90} = 0.706 \times OV_{Todorov} \approx 5,585,000 \text{ bbl}$$

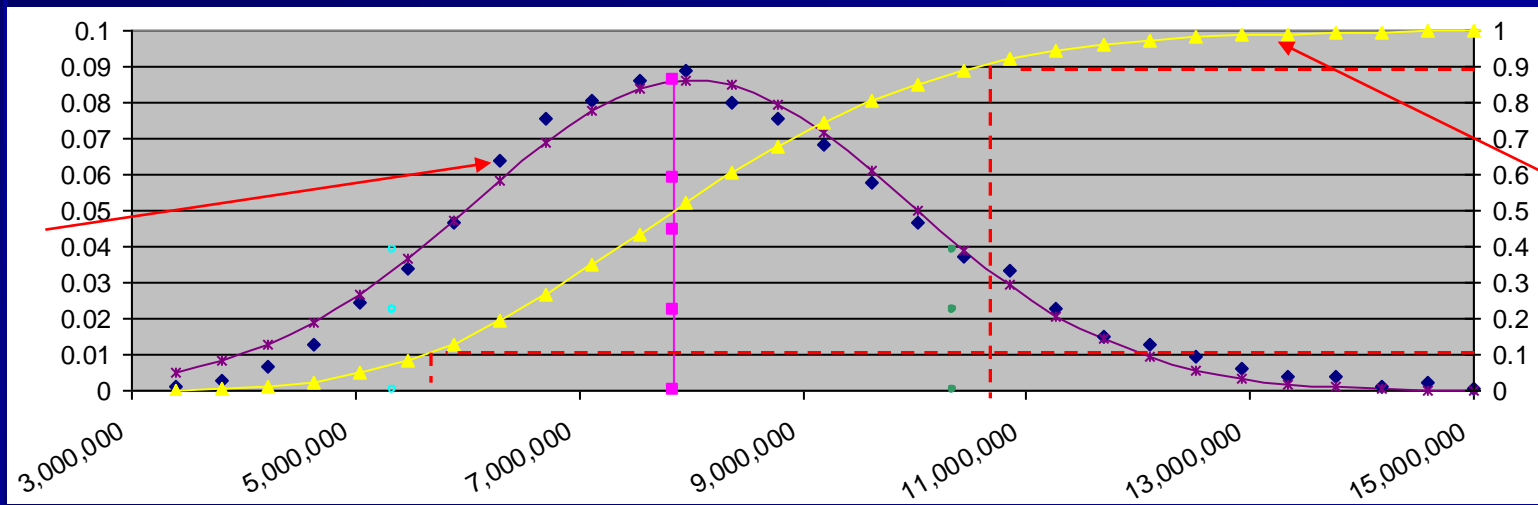
$$P_{10} = 1.294 \times OV_{Todorov} \approx 10,235,000 \text{ bbl}$$

# Monte Carlo approach

- $OV = \text{thickness} \times \% \text{sand} \times \phi \times (1 - S_{wi}) \times \text{Area}$
- 10,000 simulations

PDF

CDF



bbl

$$P_{90} = 5,700,000 \text{ bbl}$$
$$P_{10} = 10,612,000 \text{ bbl}$$


# Conclusions & Future work

- A total uncertainty was associated with the OV prediction
- A probability was associated with the OV prediction
- Quantification of the contribution of geophysical information used in the OV prediction should be done

- **Picking uncertainty**

$$t_e = \frac{1}{f_m \log_2 \left[ 1 + \left( \frac{S}{N} \right)^2 \right]}$$

Stewart et al. 1984


$$SSE(f) = SS(f) \sqrt{SD \cdot NR \cdot NA}$$

Meunier, 2011